# Einführung in die Computerlinguistik Statistical Natural Language Processing

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Schütze & Zangenfeind: Statistical Natural Language Processing

#### • Statistical Natural Language Processing (StatNLP): Introduction

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- Noisy channel model: early work was based on understanding StatNLP as "decoding messages"

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- Noisy channel model: early work was based on understanding StatNLP as "decoding messages"
- Language models: probability models that distinguish more vs less likely word sequences

#### Outline







#### Unser Plan

- Teilgebiete der Linguistik
  - Phonetik und Phonologie
  - Morphologie
  - Syntax
  - Semantik
  - Pragmatik
- Statistische Sprachverarbeitung

#### Outline



2 Noisy channel model



# Statistical Natural Language Processing

### Statistical Natural Language Processing

#### Definition

Statistical Natural Language Processing (StatNLP) uses methods of supervised, semisupervised and unsupervised learning to address tasks that involve written or spoken (human) language.

# What does "statistical" mean?

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#### Adjective for "statistics"

 $\mathsf{statistics} = \mathsf{the}\ \mathsf{practice}\ \mathsf{or}\ \mathsf{science}\ \mathsf{of}\ \mathsf{collecting}\ \mathsf{and}\ \mathsf{analyzing}\ \mathsf{numerical}\ \mathsf{data}$ 

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an important / the most important subfield of machine learning also a subject of statistics, but the emphasis is different

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- automatic summarization of text
- sentiment analysis (e.g., find all *negative* reviews of the smartphone I want to buy)

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#### Applications that use some StatNLP

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#### Applications that use some StatNLP

speech recognition

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#### Applications that use some StatNLP

speech recognition optical character recognition

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# History of StatNLP (simplified)

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- 2000s: The field splits methodologically into three communities.
  - traditional computational linguistics
  - a large group of researchers that use simple statistical methods
  - a small group of researchers that do active research on machine learning methods

### Recent big success story 1
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## Recent big success story 2

## Recent big success story 2

#### Siri. Your wish is its command.

Siri on iPhone 45 lets you use your voice to send messages, schedule meetings, place phone calls, and more. Ask Siri to do things just by taking the way you talk. Siri understands what you say, knows what you mean, and even talks back. Siri is so easy to use and does so much, you'll keep finding more and mare ways to use it.



What is StatNLP? Noisy channel model Language models

#### Recent big success story 3

#### Google Translate - more on this later

#### Outline







## Fred Jelinek

# Fred Jelinek



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Well-known examples of applications of noisy channel model?



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# Noisy (actually, non-noisy) channel example: T9

Decode 788884278

What is StatNLP? Noisy channel model Language models

## Conditional probability

What is StatNLP? Noisy channel model Language models

## Conditional probability

• The conditional probability is the updated probability of an event given some knowledge.

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# • Definition: $P(A|B) = \frac{P(A \cap B)}{P(B)} (P(B) > 0)$



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#### Exercise



Compute P(A|B) = P(AB)/P(B) and P(B|A) = P(AB)/P(A)

## Bayes' theorem

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## • Follows from $P(A) = P(A \cap B) + P(A \cap \overline{B}) = P(A|B)P(B) + P(A|\overline{B})P(\overline{B})$

## Independence

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• 
$$P(A) = P(A|B), P(B) = P(B|A)$$

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- Why  $\approx$ ?

What is StatNLP? Noisy channel model Language models

### Testing for independence: Example

#### A = champagne, B = sparkling

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What is StatNLP? Noisy channel model Language models

### Testing for independence: Exercise

### (a) compute numbers for a pair of words of your choice; (b) find two independent words

Cooccurrence counts of the words tree and missile. E.g., there are 10 documents that contain both tree and missile; there are 100 documents that contain missile and do not contain tree.

tree not tree missile 10 100 not missile 1000 ?

Replace the question mark in the table by a number that makes the two words independent of each other.

### IBM Watson approach to NLP

- sequence model
- in most cases: given an observation, select the most likely sequence that caused the observation
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- word sequence: sequence of words
- evidence: acoustic signal
- P(evidence|word-sequence): a model of how humans translate a sequence of (written) words into acoustics

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- word sequence: sequence of words
- evidence: image
- P(evidence|word-sequence): a model of how a machine (e.g., a desktop printer) translates a sequence of words into printed letters/symbols



### Build a noisy channel machine translation model for translating French into English.

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=	argmaxword-sequence	$\frac{P(\text{evidence} \text{word-sequence})P(\text{word-sequence})}{P(\text{evidence})}$	word-sequence)
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 $argmax_{word-sequence} P(word-sequence|evidence)$   $= argmax_{word-sequence} \frac{P(evidence|word-sequence)P(word-sequence)}{P(evidence)}$   $= argmax_{word-sequence} P(evidence|word-sequence) P(word-sequence)$ 

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- word sequence: sequence of English words
- evidence: sequence of French words
- P(evidence|word-sequence): a model of how humans translate a sequence of English words into a sequence of French words

### Noisy channel: Information theory / telecommunications



### Noisy channel: Speech recognition



### Noisy channel: Optical character recognition



### Noisy channel: French-to-English machine translation



### The two key components of the model

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= argmax<sub>word-sequence</sub> P(evidence|word-sequence) P(word-sequence)

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### How to build a translation model

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- Compute a word alignment for the parallel corpus (next slide)
- Estimate a translation model from the word alignment (that is, the model that models how humans generate French sentences from English sentences)
- Also: need a decoding/search algorithm because the search space is huge

# Estimating word translation probabilities



Estimate:  $P(e_i | \text{nouvelles})$   $P(f_j | \text{fees})$   $P(f_j | \text{the})$  $P(f_j | e_0)$ 

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# "Linguistic" word/phrase alignment of a parallel corpus

What is StatNLP?

# "Linguistic" word/phrase alignment of a parallel corpus



 $p(f|e) \propto \sum_{a_1=0}^{l} \cdots \sum_{a_m=0}^{l} p(\langle a_1, \dots, a_m \rangle) \prod_{j=1}^{m} p(f_j|e_{a_j})$ 

$$p(f|e) \propto \sum_{a_1=0}^{l} \cdots \sum_{a_m=0}^{l} p() \prod_{j=1}^{m} p(f_j|e_{a_j})$$

• e: English sentence,  $e_i$ :  $i^{th}$  word in e

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- e<sub>aj</sub> is the English word that f<sub>j</sub> is aligned with this assumes that the alignment is a (total) function:
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- $p(f_j|e_{a_j})$  is the probability of  $e_{a_j}$  being translated as  $f_j$ .

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### Estimating word translation probabilities



Estimate:  $P(e_i | \text{nouvelles})$   $P(f_j | \text{fees})$   $P(f_j | \text{the})$  $P(f_j | e_0)$ 

Schütze & Zangenfeind: Statistical Natural Language Processing

$$p(f|e) \propto \sum_{a_1=0}^{l} \cdots \sum_{a_m=0}^{l} p(\langle a_1, \ldots, a_m \rangle) \prod_{j=1}^{m} p(f_j|e_{a_j})$$

- e: English sentence, e<sub>i</sub>: i<sup>th</sup> word in e
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- f: French sentence,  $f_i$ :  $j^{th}$  word in f
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# Formalization of alignment

$e_0 e_1 e_2$ empty cept they descended									
$f_1$ $f_2$ runter gingen		f <sub>3</sub> sie			J				
a <sub>1</sub>	a <sub>2</sub>	a <sub>3</sub>	a <sub>1</sub>	a <sub>2</sub>	a <sub>3</sub>		$a_1$	a <sub>2</sub>	a <sub>3</sub>
0	0	0	1	0	0		2	0	0
0	0	1	1	0	1		2	0	1
0	0	2	1	0	2		2	0	2
0	1	0	1	1	0		2	1	0
0	1	1	1	1	1		2	1	1
0	1	2	1	1	2		2	1	2
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# What's bad about this model? What type of linguistic phenomenon will not be translated correctly?

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What is StatNLP? Noisy channel model Language models

# What's bad about this model (2)

#### • Morphology: "Kind" - "Kindes"

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- Syntax: which types of differences between German syntax and English syntax could be a problem?

# Google Translate

#### Exercise

Devise a set of rules that will translate words like *flanierst*, *garniert*, and *Kiefer* correctly. Devise a set of rules that will handle case correctly. Devise a set of rules that will handle long-distance dependencies correctly.
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- Phrase alignment instead of word alignment

Morphology

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linguistic syntax as well as data-driven automatic bracketing

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#### Outline







# The two key components of the model



#### Noisy channel: French-to-English machine translation



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- We'll choose "recognize speech" based on this.

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Example:

$$p_{\mathrm{ML}}(\mathsf{be}|\mathsf{would}) = rac{C(\mathsf{would be})}{C(\mathsf{would})} = rac{18454}{83735} pprox 0.22$$

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- This means that in machine translation, any English sentence containing "Dr. Cooper" would be deemed impossible and could not be output by the translator.
- This problem is called sparseness.
- Ideally, we would need knowledge about events and their probability that never occurred in our training corpus.

### Laplace

$$p_L(w_2|w_1) = \frac{C(w_1w_2)+1}{C(w_1)+|V|}$$

where C(e) is the number of times the event e occurred in the training set, V is the vocabulary of the training set and  $w_{i,j}$  is the sequence of words  $w_i, w_{i+1}, \ldots, w_{j-1}, w_j$ .

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Better estimator:

$$p_L(\text{Cooper}|\text{Dr.}) = \frac{0+1}{10000 + 256873} \approx 0.0000037 \rangle 0$$

So now our machine translation system has a chance of finding a good English translation that contains the phrase "Dr. Cooper".

## Laplace: Better, but not great

$$p_{\mathrm{ML}}(\mathrm{be}|\mathrm{would}) = rac{C(\mathrm{would be})}{C(\mathrm{would})} = rac{18454}{83735} pprox 0.22$$
 $p_L(\mathrm{be}|\mathrm{would}) = rac{18454 + 1}{83735 + 256873} pprox 0.05$ 

#### Exercise

# the three women saw the small mountain behind the large mountain

Compute maximum likelihood and laplace estimates for: p(three|the) and p(saw|the)

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- We have looked at a bigram model, order = 2.
- In many applications, notably in machine translation, language models of higher order are used: 7-gram, 8-gram, 9-gram models.

### Take-away

- Statistical Natural Language Processing (StatNLP): Introduction
- Noisy channel model: early work was based on understanding StatNLP as "decoding messages"
- Language models: probability models that distinguish more vs less likely word sequences